

# OCR

Oxford Cambridge and RSA

## Wednesday 14 June 2017 – Morning

### AS GCE MATHEMATICS (MEI)

4771/01 Decision Mathematics 1

#### QUESTION PAPER

Candidates answer on the Printed Answer Book.

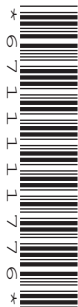
**OCR supplied materials:**

- Printed Answer Book 4771/01
- MEI Examination Formulae and Tables (MF2)

**Other materials required:**

- Scientific or graphical calculator

**Duration:** 1 hour 30 minutes



#### INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the Printed Answer Book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the barcodes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

#### INFORMATION FOR CANDIDATES

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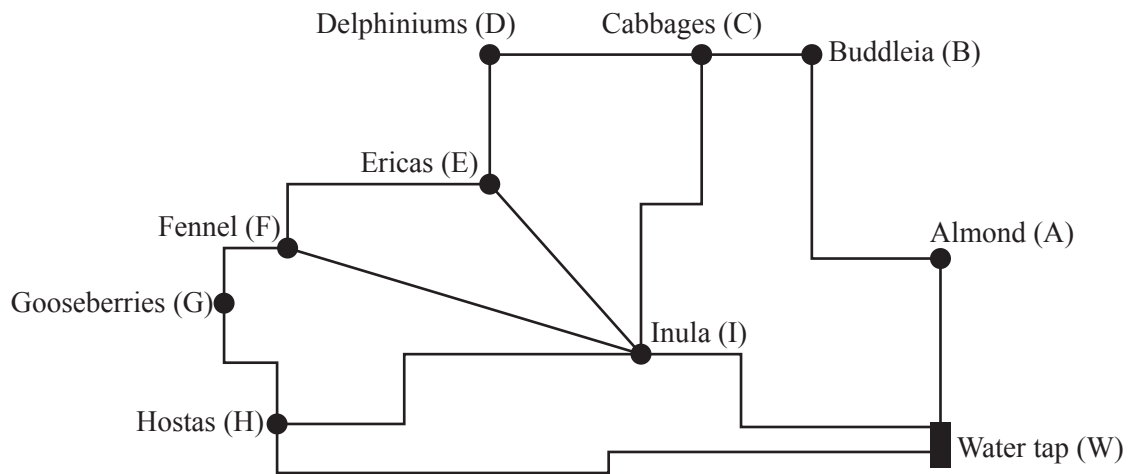
- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- The Printed Answer Book consists of **12** pages. The Question Paper consists of **8** pages. Any blank pages are indicated.

#### INSTRUCTIONS TO EXAMS OFFICER/INVIGILATOR

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## Section A (24 marks)

- 1 Pippa is planning an irrigation system for a new garden. The graph shows the water tap, the plants and trees which need to be watered, and possible routes for the irrigation pipes.



The lengths of possible pipe runs (m) are given in the table.

|   | W  | A  | B  | C  | D  | E  | F  | G | H  | I  |
|---|----|----|----|----|----|----|----|---|----|----|
| W |    | 10 |    |    |    |    |    |   | 40 | 20 |
| A | 10 |    | 17 |    |    |    |    |   |    |    |
| B |    | 17 |    | 7  |    |    |    |   |    |    |
| C |    |    | 7  |    | 12 |    |    |   |    | 18 |
| D |    |    |    | 12 |    | 8  |    |   |    |    |
| E |    |    |    |    | 8  |    | 14 |   |    | 11 |
| F |    |    |    |    |    | 14 |    | 5 |    | 15 |
| G |    |    |    |    |    |    | 5  |   | 6  |    |
| H | 40 |    |    |    |    |    |    | 6 |    | 18 |
| I | 20 |    |    | 18 |    | 11 | 15 |   | 18 |    |

- (i) Starting at W, use Prim's algorithm in tabular form to find the least length of pipe that is needed for the system. Give the length of pipe and draw the connections that are used in this solution. [5]

In fact, Pippa decides to connect the Inula directly to the water tap and then to use all of the direct connections from the Inula. The Almond, Buddleia, Delphiniums and Gooseberries she will subsequently connect in optimally.

- (ii) Draw Pippa's connections. Give the minimum length of pipe she will need for this solution, and give a reason why she might choose it. [3]

2 The following is an algorithm for 'shop subtraction'. It applies to two whole numbers, each between 0 and 999.

10 Let P be the smaller number

20 Let M be the larger number

30 Let C be 0

40 If  $P + C + 100 > M$  then goto 70

50 Let  $C = C + 100$

60 Goto 40

70 If  $P + C + 10 > M$  then goto 100

80 Let  $C = C + 10$

90 Goto 70

100 If  $P + C + 1 > M$  then goto 130

110 Let  $C = C + 1$

120 Goto 100

130 Print 'The answer is' C

- (i) Apply the algorithm to the numbers 112 and 250. Show the steps as you apply them and give the answer. [4]
- (ii) Show how to modify the algorithm so that it can be applied to numbers between 0 and 9999. [3]
- (iii) What is the connection between the algorithm and giving change for a purchase made in a shop? [1]

**3**  $K_{2,4}$  is the complete bipartite graph on sets of 2 and 4 elements, i.e. all possible ways of joining 2 elements in one set to 4 elements in another set.

**(i)** Draw  $K_{2,4}$  with no lines crossing. [1]

**(ii)** Explain how  $K_{2,n}$  can be drawn without any lines crossing for any positive integer  $n$ . [1]

**(iii)** The smallest value of  $n$  for which  $K_{3,n}$  cannot be drawn without any lines crossing is  $n = 3$ . Start from a drawing of  $K_{2,3}$  and explain why it is not possible to construct  $K_{3,3}$  from this without having any lines crossing. [3]

It is claimed that the minimum number of line crossings needed to draw  $K_{3,n}$  is given by  $\frac{(n-1)^2}{4}$  if  $n$  is odd and  $\frac{n(n-2)}{4}$  if  $n$  is even.

**(iv)** Draw  $K_{3,5}$  with the number of line crossings given by the formula. [2]

**(v)** Explain the consequences of parts (i) to (iv) for circuit board design. [1]

**Section B** (48 marks)

- 4 A nursery has  $9000\text{m}^2$  of land available for growing deciduous trees and evergreen trees from saplings (young trees). Each deciduous tree needs  $8\text{m}^2$  of space, and each evergreen tree needs  $6\text{m}^2$  of space.

The costs of purchasing saplings, labour, fertilisers, etc. are £16 for each deciduous tree and £16 for each evergreen tree, and £20 000 is available to invest.

The nursery can obtain at most 800 deciduous saplings for planting, and at most 1000 evergreen saplings.

When the saplings have grown into trees, the nursery sells the deciduous trees for £25 each, and the evergreen trees for £22 each.

- (i) Calculate the profit which will be made from each deciduous tree and from each evergreen tree. [1]

The nursery manager wants to find how many trees of each type should be grown so as to maximise the profit.

- (ii) Formulate the manager's problem as a linear program, ignoring the fact that the numbers of trees must be integers. [5]

- (iii) Draw the feasible region for your problem in part (ii), and hence show that the solution to the LP is 800 deciduous trees and  $433\frac{1}{3}$  evergreen trees. Give the maximum profit. [7]

- (iv) How much extra profit would be made for an extra  $100\text{m}^2$  of land, still allowing for non-integer solutions?

How much extra profit (compared to your answer to part (iii)) would be made for an extra  $1000\text{m}^2$  of land, still allowing for non-integer solutions? [2]

- (v) Saplings have to be purchased in bundles of 50 at a time. For the original problem, with  $9000\text{m}^2$  of land available, find the optimal number of each type of sapling to purchase. [1]

- 5 John wants to generate integers between 0 and 15, each being equally likely. He has a coin available. He constructs a table with headings as shown, and with as many rows as he needs.

| 8   | 4 | 2 | 1 |
|-----|---|---|---|
|     |   |   |   |
|     |   |   |   |
| ... |   |   |   |
|     |   |   |   |

To complete the first row he throws the coin four times, recording the results as a 1 for ‘heads’ or a 0 for ‘tails’ in the four columns of the first row, starting from the right and moving left. For example, if he gets two heads, then a tail and then another head, this will be recorded in the table as 1, 0, 1, 1 (remembering that the order is from the right). He then multiplies the entries in the row by the column headings to get a score. In the example the score is  $8 + 2 + 1 = 11$ .

So the example has the following result and score:

| 8   | 4 | 2 | 1 |
|-----|---|---|---|
| 1   | 0 | 1 | 1 |
|     |   |   |   |
| ... |   |   |   |
|     |   |   |   |

11

- (i) Explain why this method generates the scores 0 to 15, each with the same probability. [3]

John wants to repeat this experiment 64 times. His last 8 coin throws are as follows:

H T T T T H T H

- (ii) Compute John’s final two scores. [2]

John is trying to simulate a fairground game in which 16 jars are arranged in a square formation, and a ball is repeatedly thrown until it lands in one of them.

(The jars have been numbered to help in the rest of this question.)

|    |    |    |    |
|----|----|----|----|
| 00 | 01 | 02 | 03 |
| 04 | 05 | 06 | 07 |
| 08 | 09 | 10 | 11 |
| 12 | 13 | 14 | 15 |

When John produces a score, that score corresponds to the number of a jar.

- (iii) Explain why John’s simulation will not be a good model of reality. [1]

John decides instead to use two-digit random numbers to simulate the game. He decides that he will allocate a probability of  $\frac{1}{36}$  for a ball to land in each of the corner jars (jars 00, 03, 12 and 15), a probability of  $\frac{2}{36}$  for each of the other eight edge jars (jars 01, 02, 04, 07, 08, 11, 13 and 14), and a probability of  $\frac{4}{36}$  for each of the other four jars.

- (iv) Give a rule for John to use, i.e. specify which jar should be represented by each two-digit random number. **[8]**
- (v) Use your rule together with the string of two-digit random numbers in the answer book to simulate two repetitions of the game. **[2]**

- 6 Pippa owns a garden construction company. She is preparing a quotation for constructing a garden on a  $1000\text{ m}^2$  site. Her quotation will need to include an estimate of how long the construction will take.

The tasks, together with limitations on their starting times and durations, are as follows:

- A Produce a detailed survey of the site. This must be done before anything else, except that clearing the site can be started at the same time. The surveying will take 1 day.
- B Clear the site. This will take 3 days.
- C Put forward a plan, debate it and adjust it. This can't be done until the survey is complete. It involves meeting with the client, and will take 3 days.
- D Build walls and other fixed features. This cannot be started until the site is cleared and the plan agreed. It will take 3 days.
- E Have a specialist contractor install the pond. This cannot be started until the site is cleared and the plan agreed. It will take 5 days.
- F Plant the trees. This cannot be started until the walls and other fixed features are completed. It will take 3 days.
- G Plant the plants. This cannot be started until the walls and other fixed features are completed. It will take 2 days.
- H Install the irrigation. This cannot be started until the trees are planted and the plants are planted. It will take 2 days.

(i) Draw an activity-on-arc precedence network for this project. [4]

(ii) Complete a forward pass and a backward pass to determine the minimum completion time and the critical activities, using the durations given above. [6]

Activities D and E will be contracted to specialist companies. Pippa plans to complete activities A, B, C, F, G and H herself, but she can employ her friend, Afzal, to do or to help with any of these tasks except for A and C. Each of B, F, G and H can be done by two people, with the total time taken by the two of them being the same as the activity duration.

(iii) The project is to be completed in the shortest time. Produce a schedule to achieve this whilst using as little of Afzal's time as possible. Show who does what and when. Give the minimum completion time and give the total time for which Afzal must be employed. [5]

(iv) How long will it take to complete the project if Pippa does not use Afzal at all? [1]

### END OF QUESTION PAPER

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**Duration:** 1 hour 30 minutes



|                       |  |                      |  |
|-----------------------|--|----------------------|--|
| Candidate<br>forename |  | Candidate<br>surname |  |
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| Centre number |  |  |  |  |  | Candidate number |  |  |  |  |
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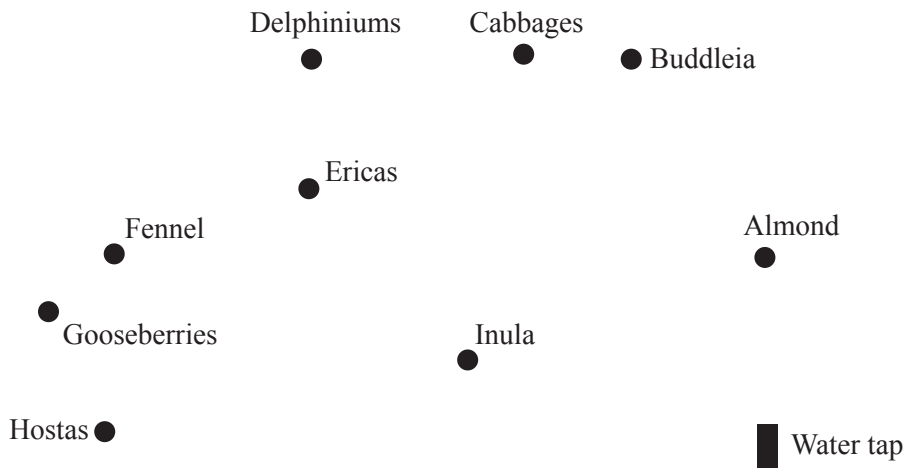
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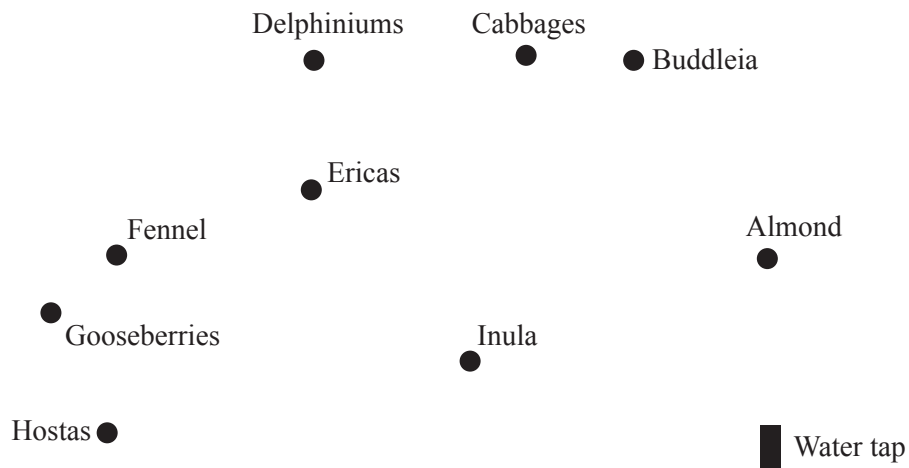
1 (i)

|   | W  | A  | B  | C  | D  | E  | F  | G | H  | I  |
|---|----|----|----|----|----|----|----|---|----|----|
| W |    | 10 |    |    |    |    |    |   | 40 | 20 |
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| E |    |    |    |    | 8  |    | 14 |   |    | 11 |
| F |    |    |    |    |    | 14 |    | 5 |    | 15 |
| G |    |    |    |    |    |    | 5  |   | 6  |    |
| H | 40 |    |    |    |    |    |    | 6 |    | 18 |
| I | 20 |    |    | 18 |    | 11 | 15 |   | 18 |    |

Length of pipe used =



1 (ii)



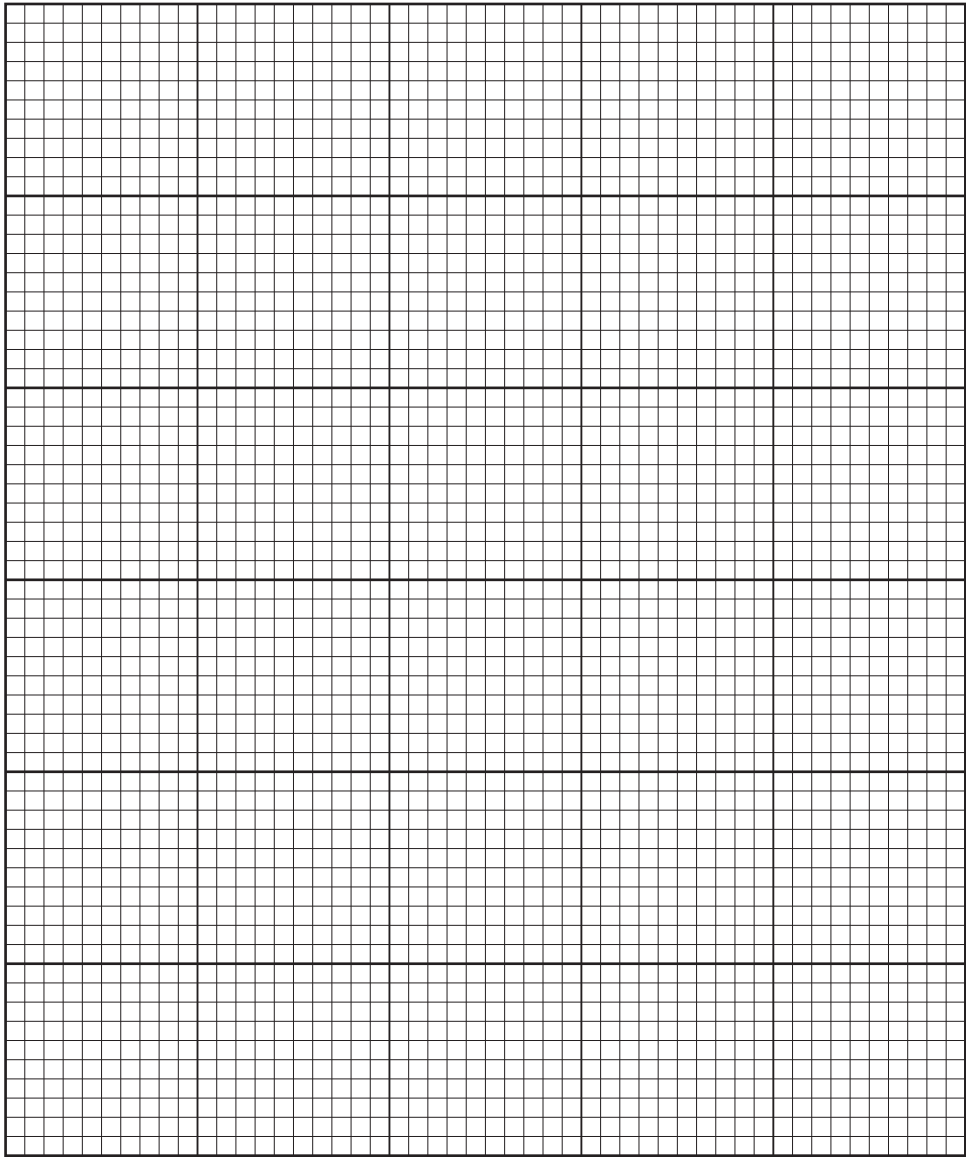
Minimum length of pipe:

Reason:

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| <b>3 (i)</b>   | <p style="text-align: center;">●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●</p> |
| <b>3 (ii)</b>  | <hr/> <hr/> <hr/> <hr/> <hr/> <hr/> <hr/>   |
| <b>3 (iii)</b> | <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●      ●</p> <hr/> <hr/> <hr/>             |

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| <b>3(iv)</b> | <p style="text-align: center;">●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●      ●</p> <p style="text-align: center;">●</p> |  |  |  |  |  |  |
| <b>3(v)</b>  | <table border="1"><tr><td> </td></tr><tr><td> </td></tr><tr><td> </td></tr><tr><td> </td></tr><tr><td> </td></tr><tr><td> </td></tr></table>  |  |  |  |  |  |  |
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| <b>4 (i)</b>   |   |
| <b>4 (ii)</b>  |   |
| <b>4 (iii)</b> | <p>A spare copy of this graph can be found on page 11.</p>  <p>(answer space continued on next page)</p> |

|                |                  |
|----------------|------------------|
| <b>4 (iii)</b> | <b>continued</b> |
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| <b>4 (iv)</b>  |                  |
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| <b>4 (v)</b>   |                  |
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| <b>5 (iii)</b> |  |
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| <b>5 (iv)</b>  |  |
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**5(v)** Two-digit random numbers:

01 99 52 67 23 62 85

6 (i) &  
(ii)

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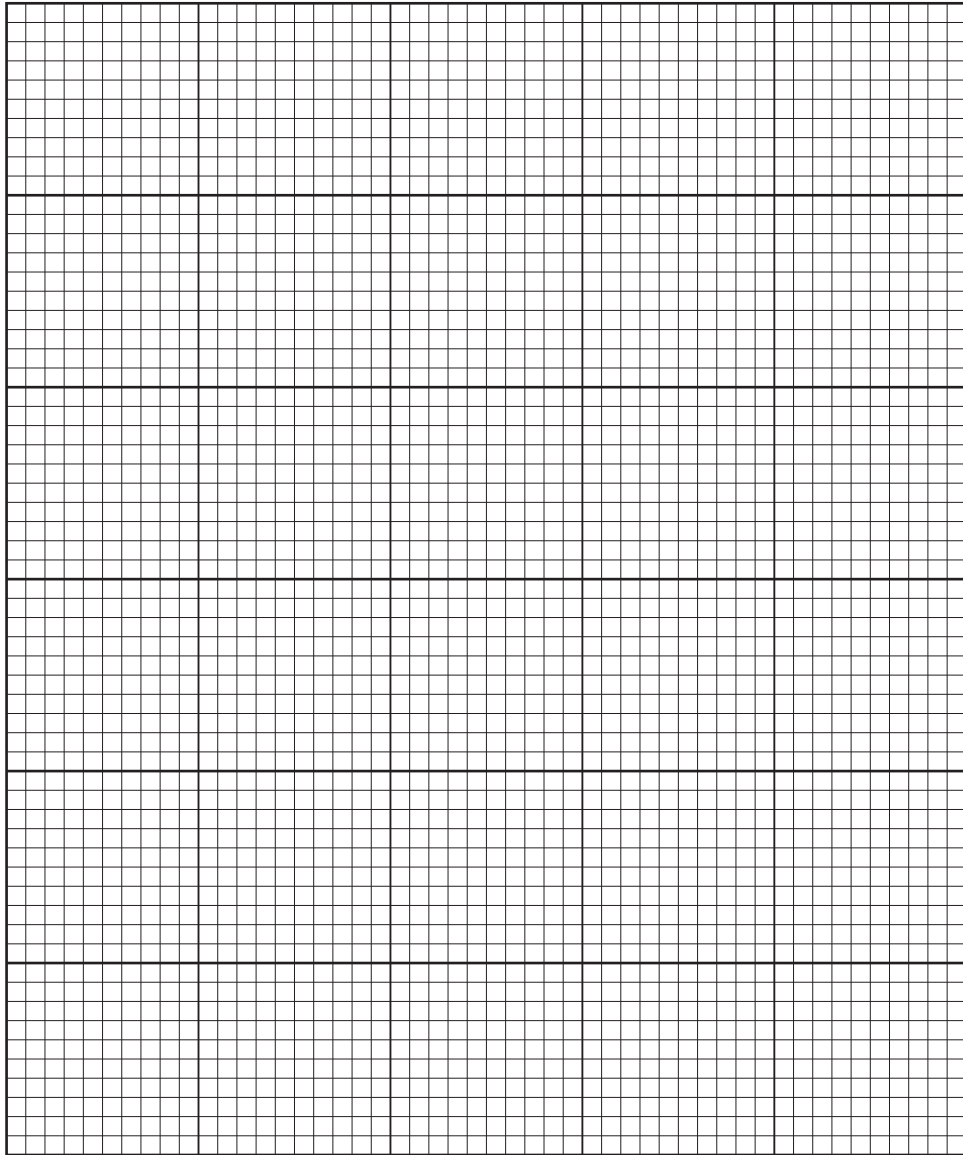
6 (iii)

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6 (iv)

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4(iii) Spare copy of graph for question 4(iii)



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**GCE**

**Mathematics (MEI)**

Unit **4771**: Decision Mathematics 1

Advanced Subsidiary GCE

**Mark Scheme for June 2017**

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

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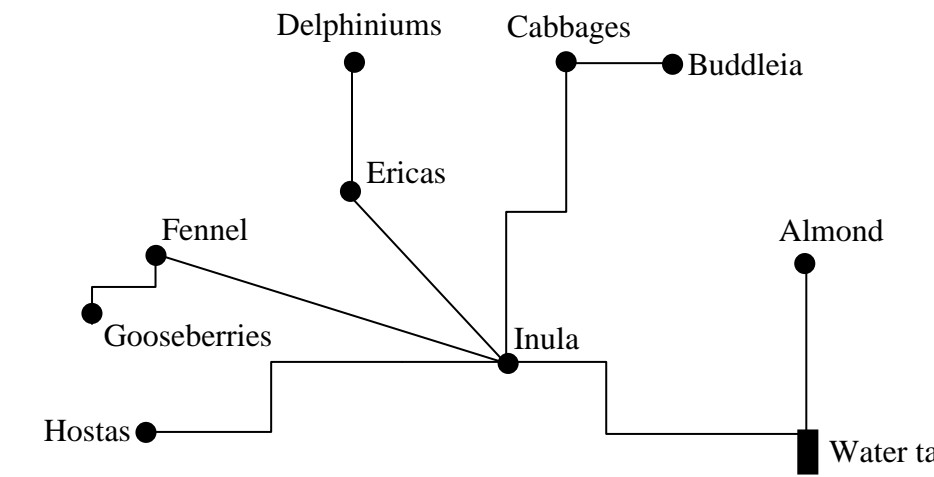
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## Annotations and abbreviations

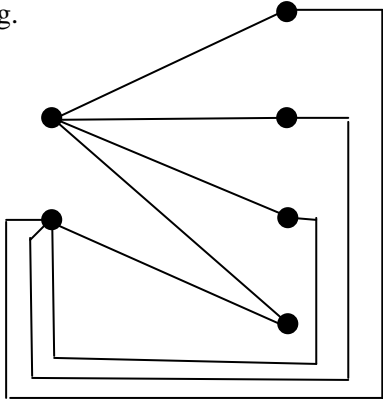
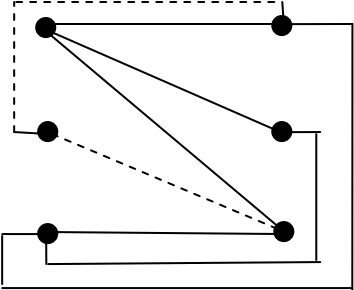
| <b>Annotation in scoris</b>               | <b>Meaning</b>   |
|---|--|
| ✓ and ✖                                   |  |
| BOD                                       | Benefit of doubt   |
| FT  | Follow through   |
| ISW                                       | Ignore subsequent working                                |
| M0, M1                                    | Method mark awarded 0, 1                                 |
| A0, A1                                    | Accuracy mark awarded 0, 1                               |
| B0, B1                                    | Independent mark awarded 0, 1                            |
| SC  | Special case   |
| ^   | Omission sign  |
| MR  | Misread  |
| Highlighting                              |  |
|   |  |
| <b>Other abbreviations in mark scheme</b> | <b>Meaning</b>   |
| E1  | Mark for explaining                                      |
| U1  | Mark for correct units                                   |
| G1  | Mark for a correct feature on a graph                    |
| M1 dep*                                   | Method mark dependent on a previous mark, indicated by * |
| cao                                       | Correct answer only                                      |
| oe  | Or equivalent  |
| rot                                       | Rounded or truncated                                     |
| soi                                       | Seen or implied  |
| www                                       | Without wrong working                                    |
|   |  |
|   |  |

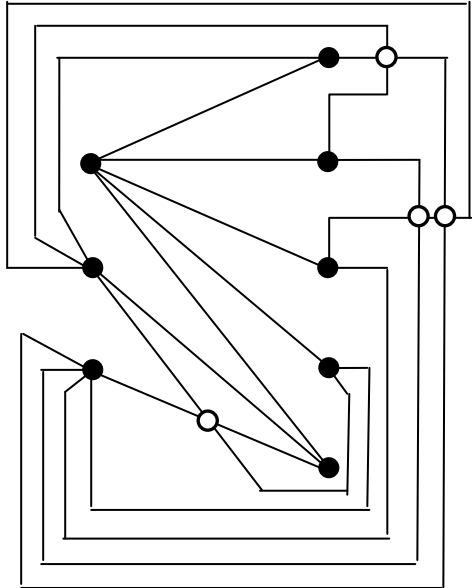
| Question | Answer  | Marks | Guidance |      |     |      |     |     |    |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
|----------|---|-------|----------|------|-----|------|-----|-----|----|----|---|----|---|--|----|--|--|--|--|--|--|----|----|---|------|--|----|--|--|--|--|--|--|--|---|--|------|--|---|--|--|--|--|--|--|---|--|--|-----|--|----|--|--|--|--|----|---|--|--|--|------|--|---|--|--|--|--|---|--|--|--|--|-----|--|----|--|--|----|---|--|--|--|--|--|------|--|---|--|----|---|--|--|--|--|--|--|-----|--|---|--|---|----|--|--|--|--|--|--|-----|--|----|---|----|--|--|----|--|------|----|--|----|--|--|--|
| 1 (i)    | <table border="1"> <thead> <tr> <th></th> <th>W1</th> <th>A2</th> <th>B3</th> <th>C4</th> <th>D5</th> <th>E6</th> <th>F8</th> <th>G9</th> <th>H</th> <th>I7</th> </tr> </thead> <tbody> <tr> <th>W</th> <td></td> <td>10</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>40</td> <td>20</td> </tr> <tr> <th>A</th> <td>(10)</td> <td></td> <td>17</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <th>B</th> <td></td> <td>(17)</td> <td></td> <td>7</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <th>C</th> <td></td> <td></td> <td>(7)</td> <td></td> <td>12</td> <td></td> <td></td> <td></td> <td></td> <td>18</td> </tr> <tr> <th>D</th> <td></td> <td></td> <td></td> <td>(12)</td> <td></td> <td>8</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <th>E</th> <td></td> <td></td> <td></td> <td></td> <td>(8)</td> <td></td> <td>14</td> <td></td> <td></td> <td>11</td> </tr> <tr> <th>F</th> <td></td> <td></td> <td></td> <td></td> <td></td> <td>(14)</td> <td></td> <td>5</td> <td></td> <td>15</td> </tr> <tr> <th>G</th> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>(5)</td> <td></td> <td>6</td> <td></td> </tr> <tr> <th>H</th> <td>40</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>(6)</td> <td></td> <td>18</td> </tr> <tr> <th>I</th> <td>20</td> <td></td> <td></td> <td>18</td> <td></td> <td>(11)</td> <td>15</td> <td></td> <td>18</td> <td></td> </tr> </tbody> </table> <p>Length of pipe used = 90m</p> <pre> graph TD     WT[Water tap] --- A[Almond]     A --- B[Buddleia]     B --- C[Cabbages]     C --- D[Delphiniums]     D --- E[Ericas]     E --- F[Fennel]     E --- G[Inula]     F --- H[Gooseberries]     H --- I[Hostas]     style WT fill:#000     </pre> |       | W1       | A2   | B3  | C4   | D5  | E6  | F8 | G9 | H | I7 | W |  | 10 |  |  |  |  |  |  | 40 | 20 | A | (10) |  | 17 |  |  |  |  |  |  |  | B |  | (17) |  | 7 |  |  |  |  |  |  | C |  |  | (7) |  | 12 |  |  |  |  | 18 | D |  |  |  | (12) |  | 8 |  |  |  |  | E |  |  |  |  | (8) |  | 14 |  |  | 11 | F |  |  |  |  |  | (14) |  | 5 |  | 15 | G |  |  |  |  |  |  | (5) |  | 6 |  | H | 40 |  |  |  |  |  |  | (6) |  | 18 | I | 20 |  |  | 18 |  | (11) | 15 |  | 18 |  | B1<br>B1<br>B1<br><br><br>B1cao<br><br>B1cao | indicating selections<br>deleting in rows<br>numbering columns<br><br><br><br><br><br><br><br><br><br><br> |
|          | W1  | A2    | B3       | C4   | D5  | E6   | F8  | G9  | H  | I7 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| W        |   | 10    |          |      |     |      |     |     | 40 | 20 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| A        | (10)  |       | 17       |      |     |      |     |     |    |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| B        |   | (17)  |          | 7    |     |      |     |     |    |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| C        |   |       | (7)      |      | 12  |      |     |     |    | 18 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| D        |   |       |          | (12) |     | 8    |     |     |    |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| E        |   |       |          |      | (8) |      | 14  |     |    | 11 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| F        |   |       |          |      |     | (14) |     | 5   |    | 15 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| G        |   |       |          |      |     |      | (5) |     | 6  |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| H        | 40  |       |          |      |     |      |     | (6) |    | 18 |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |
| I        | 20  |       |          | 18   |     | (11) | 15  |     | 18 |    |   |    |   |  |    |  |  |  |  |  |  |    |    |   |      |  |    |  |  |  |  |  |  |  |   |  |      |  |   |  |  |  |  |  |  |   |  |  |     |  |    |  |  |  |  |    |   |  |  |  |      |  |   |  |  |  |  |   |  |  |  |  |     |  |    |  |  |    |   |  |  |  |  |  |      |  |   |  |    |   |  |  |  |  |  |  |     |  |   |  |   |    |  |  |  |  |  |  |     |  |    |   |    |  |  |    |  |      |    |  |    |  |  |  |



|      |  |                            |   |
|------|--|----------------------------|---|
| (ii) |  <p data-bbox="324 774 784 837">112m<br/>Shorter runs, or less exposure to risk.</p> | M1<br><br><br><br>A1<br>B1 | 3 out of 4 connections for A, B, D and G correct<br><br><br><br>cao |
|------|--|----------------------------|---|

| Question |       | Answer   | Marks                                   | Guidance   |
|----------|-------|--|---|--|
| 2        | (i)   | <p>P 112</p> <p>M 250</p> <p>C (0) 100 110 120 130 131 132 133 134 135 136 137 138</p> <p>The answer is 138</p>                      | <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> | <p>correct to statement 100<br/>(i.e. 130)</p>                         |
|          | (ii)  | <p>e.g. add</p> <p>34 If <math>P + C + 1000 &gt; M</math> then goto 40</p> <p>35 Let <math>C = C + 1000</math></p> <p>36 Goto 34</p> | <p>B1</p> <p>B1</p> <p>B1</p>           | <p>(ignore “34” and “40”)</p> <p>(ignore “35”)</p> <p>logic all OK</p> |
|          | (iii) | <p>e.g. P = price, M = money tendered, C = change</p>  | <p>B1</p>                               | <p>No need to consider note denominations instead of powers of 10.</p> |

| Question | Answer  | Marks                         | Guidance  |
|----------|---|-------------------------------|---|
| 3 (i)    | <p>e.g.</p>    | B1                            |   |
| (ii)     | <p>e.g. as per the above, with top left connected directly and bottom left connected around the back.</p>   | B1                            |   |
| (iii)    | <p>e.g.</p>  <p>e.g.<br/>(Dotted connections not needed.)<br/>The middle left cannot access the middle right.</p> | <p>B1</p> <p>M1</p> <p>E1</p> | <p><math>K_{2,3}</math> seen</p> <p>choice of just two points that cannot be connected on the candidate's graph.</p> <p>dependent on the M1</p> |

|             |  |                     |                       |
|-------------|--|---------------------|-----------------------|
| <p>(iv)</p> | <p><math>(5-1) \times (5-1) / 4 = 4</math> crossings</p> <p>e.g.</p>  | <p>B1</p> <p>B1</p> | <p>can be implied</p> |
| <p>(v)</p>  | <p>e.g. They inform about how many layers will be needed.</p>  | <p>B1</p>           |                       |

| Question |       | Answer   | Marks                                  | Guidance  |
|----------|-------|--|--|---|
| 4        | (i)   | £9 and £6 respectively   | B1                                     |   |
|          | (ii)  | Let $x$ be the number of deciduous trees and $y$ the number of evergreens.<br>Max $9x+6y$<br>st $8x+6y<9000$<br>$16x+16y<20000$<br>$x<800$<br>$y<1000$   | B1<br>B1<br>B1<br>B1<br>B1             |   |
|          | (iii) | e.g. <p style="text-align: right;"> <math>(800, 433\frac{1}{3}) \rightarrow 9800</math>    <math>((800, 0) \rightarrow 7200)</math><br/> <math>(750, 500) \rightarrow 9750</math> </p> Profit is £9800 | B1<br>B1<br>B1<br>B1<br>B1<br>B1<br>B1 | labelling and scaling axes<br>line for space constraint<br>line for finance constraint<br>lines for availability constraints<br>feasible region indicated (with 6 or 5 lines correct)<br>for profit at $(800, 433\frac{1}{3})$ and $(750, 500)$ or gradient method with gradient $-1.5$ |
|          | (iv)  | £100 (at $(800, 450)$ )<br>£100 (also at $(800, 450)$ )  | B1<br>B1                               |   |
|          | (v)   | $(750, 500)$ or 15 and 10 bundles (giving £9750 - but this not required)   | B1                                     |   |

| Question                    |             | Answer   | Marks            | Guidance                                      |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
|-----------------------------|-------------|--|------------------|---|----|-------|---|-------------|------|----|-------|---|-------------|------|----|-------|---|-------------|--------|----|-------|---|--------------|------|----|-------|---|--------------|--------|----|-------|---|--------------|--------|----|-------|---|--------------|------|----|-------|---|--------------|------|----|-------|---|--------------|--------|----|-------|---|--------------|--------|----|-------|---|--------------|------|----|-------|---|--------------|--------|----|-------|---|--------------|------|----|-------|---|--------------|------|----|-------|---|--------------|--------|----|-------|---|-----------------------------|--------|--|-------|----|--|---|
| 5                           | (i)         | stating 0000 gives a score of 0<br>stating 1111 gives a score of 15<br>all equally likely  | B1<br>B1<br>B1   | or 16 (B1) distinct<br>numbers generated (B1) |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
|                             | (ii)        | 1<br>10  | B1<br>B1         | penultimate<br>last<br>SC1 ... 8, 5           |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
|                             | (iii)       | The ball will not have an equal probability of landing in each jar   | B1               |   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
|                             | (iv)        | <table border="0"> <tr> <td>e.g. 00, 01 → 00</td> <td>e.g. corner</td> <td>00</td> <td>00-01</td> <td>2</td> </tr> <tr> <td>02, 03 → 03</td> <td>edge</td> <td>01</td> <td>02-05</td> <td>4</td> </tr> <tr> <td>04, 05 → 12</td> <td>edge</td> <td>02</td> <td>06-09</td> <td>4</td> </tr> <tr> <td>06, 07 → 15</td> <td>corner</td> <td>03</td> <td>10-11</td> <td>2</td> </tr> <tr> <td>08 – 11 → 01</td> <td>edge</td> <td>04</td> <td>12-15</td> <td>4</td> </tr> <tr> <td>12 – 15 → 02</td> <td>inside</td> <td>05</td> <td>16-23</td> <td>8</td> </tr> <tr> <td>16 – 19 → 04</td> <td>inside</td> <td>06</td> <td>24-31</td> <td>8</td> </tr> <tr> <td>20 – 23 → 07</td> <td>edge</td> <td>07</td> <td>32-35</td> <td>4</td> </tr> <tr> <td>24 – 27 → 08</td> <td>edge</td> <td>08</td> <td>36-39</td> <td>4</td> </tr> <tr> <td>28 – 31 → 11</td> <td>inside</td> <td>09</td> <td>40-47</td> <td>8</td> </tr> <tr> <td>32 – 35 → 13</td> <td>inside</td> <td>10</td> <td>48-55</td> <td>8</td> </tr> <tr> <td>36 – 39 → 14</td> <td>edge</td> <td>11</td> <td>56-59</td> <td>4</td> </tr> <tr> <td>40 – 47 → 05</td> <td>corner</td> <td>12</td> <td>60-61</td> <td>2</td> </tr> <tr> <td>48 – 55 → 06</td> <td>edge</td> <td>13</td> <td>62-65</td> <td>4</td> </tr> <tr> <td>56 – 63 → 09</td> <td>edge</td> <td>14</td> <td>66-69</td> <td>4</td> </tr> <tr> <td>64 – 71 → 10</td> <td>corner</td> <td>15</td> <td>70-71</td> <td>2</td> </tr> <tr> <td>72 – 99 → reject and repeat</td> <td>reject</td> <td></td> <td>72-99</td> <td>28</td> </tr> </table> | e.g. 00, 01 → 00 | e.g. corner                                   | 00 | 00-01 | 2 | 02, 03 → 03 | edge | 01 | 02-05 | 4 | 04, 05 → 12 | edge | 02 | 06-09 | 4 | 06, 07 → 15 | corner | 03 | 10-11 | 2 | 08 – 11 → 01 | edge | 04 | 12-15 | 4 | 12 – 15 → 02 | inside | 05 | 16-23 | 8 | 16 – 19 → 04 | inside | 06 | 24-31 | 8 | 20 – 23 → 07 | edge | 07 | 32-35 | 4 | 24 – 27 → 08 | edge | 08 | 36-39 | 4 | 28 – 31 → 11 | inside | 09 | 40-47 | 8 | 32 – 35 → 13 | inside | 10 | 48-55 | 8 | 36 – 39 → 14 | edge | 11 | 56-59 | 4 | 40 – 47 → 05 | corner | 12 | 60-61 | 2 | 48 – 55 → 06 | edge | 13 | 62-65 | 4 | 56 – 63 → 09 | edge | 14 | 66-69 | 4 | 64 – 71 → 10 | corner | 15 | 70-71 | 2 | 72 – 99 → reject and repeat | reject |  | 72-99 | 28 | M1<br>A1<br><br>M1<br>A1<br><br>M1<br>A1<br><br>M1<br>A1 | reject some<br>efficient – numbers stated<br><br>rule for corner jars<br><br>rule for edge jars<br><br>rule for inside jars |
| e.g. 00, 01 → 00            | e.g. corner | 00   | 00-01            | 2   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 02, 03 → 03                 | edge        | 01   | 02-05            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 04, 05 → 12                 | edge        | 02   | 06-09            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 06, 07 → 15                 | corner      | 03   | 10-11            | 2   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 08 – 11 → 01                | edge        | 04   | 12-15            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 12 – 15 → 02                | inside      | 05   | 16-23            | 8   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 16 – 19 → 04                | inside      | 06   | 24-31            | 8   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 20 – 23 → 07                | edge        | 07   | 32-35            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 24 – 27 → 08                | edge        | 08   | 36-39            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 28 – 31 → 11                | inside      | 09   | 40-47            | 8   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 32 – 35 → 13                | inside      | 10   | 48-55            | 8   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 36 – 39 → 14                | edge        | 11   | 56-59            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 40 – 47 → 05                | corner      | 12   | 60-61            | 2   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 48 – 55 → 06                | edge        | 13   | 62-65            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 56 – 63 → 09                | edge        | 14   | 66-69            | 4   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 64 – 71 → 10                | corner      | 15   | 70-71            | 2   |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |
| 72 – 99 → reject and repeat | reject      |  | 72-99            | 28  |    |       |   |             |      |    |       |   |             |      |    |       |   |             |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |              |        |    |       |   |              |      |    |       |   |              |        |    |       |   |              |      |    |       |   |              |      |    |       |   |              |        |    |       |   |                             |        |  |       |    |  |   |

|  |     |  |       |                             |
|--|-----|--|-------|-----------------------------|
|  | (v) | e.g. Using the above rule(s), the first ball lands in jar 00 (00) and the second in jar 06 (10). | B1 B1 | √ subject to last 3 M marks |
|--|-----|--|-------|-----------------------------|

| Question | Answer  | Marks  | Guidance   |
|----------|---|--|--|
| 6 (i)    | <p>e.g.</p>   | <p>M1<br/>A1<br/>A1<br/>A1</p>               | <p>activity-on-arc<br/>A, B, C<br/>D, E<br/>Rest</p> |
| 6 (ii)   | <p>e.g.</p> <p>minimum completion time – 12 days<br/>critical activities – A, C, D, F, H.</p> | <p>M1<br/>A1<br/>M1<br/>A1<br/>B1<br/>B1</p> | <p>forward pass<br/>backward pass</p>                |

|                       |                |  |  |                                     |
|-----------------------|----------------|--|--|-------------------------------------|
| <p><b>6 (iii)</b></p> | <p>e.g.</p>    | <div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> <p>5                      10</p> </div> <div> <ul style="list-style-type: none"> <li> Pippa</li> <li> Afzal</li> <li> Building contractor</li> <li> Pond contractor</li> </ul> </div> </div> <p>Minimum completion time = 10.5 days<br/>Afzal needs to be employed for 6.5 days.</p> | <p>B1<br/>B1<br/>B1<br/><br/>B1<br/>B1</p> | <p>A, B, C<br/>D, E<br/>F, G, H</p> |
| <p><b>6 (iv)</b></p>  | <p>17 days</p> |  | <p>B1</p>                                  |                                     |



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## 4771 Decision Mathematics 1

### General Comments:

There were a number of candidates for this paper who exhibited very poor communication skills. Candidates who did not take the time to read the questions carefully, and who did not express their answers clearly, could not do well on this paper.

Many of the general comments from last year's report resonate with this year's scripts.

There were very significant difficulties with respect to accurate and concise communication which are affecting the quality of the mathematics presented by some candidates.

Having said that, there were cases in which candidates moved from very poor communication in, for instance, the explanation required in 3(ii), to excellent answers to subsequent algorithmic work. Candidates would benefit from more emphasis on the "explain" element, an emphasis which should not be restricted to preparing for examinations in decision mathematics.

### Comments on Individual Questions:

#### Question No.1

Many candidates had difficulties with applying the algorithm in part (i). It was very common to see FI selected at the end instead of FE. This proved to be expensive in terms of marks lost, in considering the context of the question it should be obvious when drawing the network that it is better to connect in F directly to E rather than to I.

A minor mistake, often seen, was to fail to number the columns following the inclusion of nodes.

There were many cases where candidates who made a good attempt at part (i) struggled with part (ii). A common minor error was to connect A to B instead of to W.

The last mark was more difficult. We have been trying to discourage fanciful answers to these interpretational parts, but we still see them. It may well be the case, for instance, that a rare spider is nesting on the direct route from A to C, diverting both arachnophiles and arachnophobes, but no marks will be awarded for supposing thus. The mark is for interpretational work on the maths, and not for creative thinking. In this case the preferred answer was to increase the resilience of the system to pipe bursts.

[For the probabilists, and certainly not required, if we assume a constant risk of breakage along the entire length of pipe, then the expected number of plants downstream from a burst is  $5\frac{1}{15}$  in the answer to (i) and  $2\frac{9}{14}$  in the answer to (ii).]

Many candidates offered "shorter pipe runs", and this was accepted as a proxy for the above. Others offered answers rooted in physics such as higher pressures or faster delivery of water, which were ultra vires.

#### Question 2

Candidates were very good indeed in following this algorithm, but not so good in the mechanics of answering the question. Many answers to part (i) were very long indeed, with much writing, often on several continuation sheets. A table of values does the job quickly and efficiently.

Most candidates scored 2 out of 3 in part (ii) because they did not know the convention of labelling in tens so that other statements can be inserted. Some resorted to writing out a whole new algorithm, incorporating their insertions and still labelling in tens.

A large proportion of candidates were not awarded the mark for part (iii) because they did not answer the question. Some wrote mini essays about proffering money to pay the price and collecting change, but failed to link P to price, M to money and C to change.

### Question No. 3

There were many very good answers to this question, except for part (v), and except for candidates who had forgotten about bipartite graphs. In part (iii) the instruction to start from  $K_{2,3}$  was helpful, and most candidates who did that were able to put together a convincing argument, which was pleasing.

The drawing required in part (iv) was intricate, and it was pleasing to see so many good attempts.

In contrast very few creditable answers were seen to part (v). This question did not require an extensive knowledge of electronics, there was enough in the question to deduce what was needed. If it can't be done in the plane then either go into 3-D (layers) or insulate your crossings – which is the same thing really. Instead most candidates accepted planarity as a constraint, and wrote about what could not be connected together on a (printed) circuit board.

### Question No. 4

The LP was really well done, particularly the graph. Candidates did well in extracting the information from the text, although there were one or two “pinch points”.

Part (i) was meant as a helpful hint, but in the event there were many candidates who correctly computed £9 and £6 for the profits in part (i) and then proceeded to use a profit function of  $25x + 22y$  in the rest of the question.

Some candidates failed to label their axes. A few used non-uniform scales and a few used poor scales, e.g. 2cm representing 300. A few did not include the origin, using instead a false origin - but they invariably incorrectly used their lower and left boundary lines as if they were axes. A few failed accurately to compute  $6 \times 433\frac{1}{3}$ . However, in general, the graphical work was done with great competence.

The interpretational work in (iv) and (v) was challenging, and it was pleasing to see some good answers.

### Question No. 5

The quality of answers to part (i) was mixed. We looked for 0000 and for 1111, and for a recognition that the equal probabilities for a head and a tail on the coin tossing leads, via the binary count, to an equal probability for each possible number. For instance, identifying  $2^4$  outcomes and 16 numbers earned the mark.

Despite the range of 0 to 15 being given in the question, quite a few candidates started counting at 1, often referring to probabilities of  $1/15$  in their explanations.

The modelling question in part (iii) prompted some essays and some misdirected consideration of the differences between game participants. All that was needed was the observation that the probability of a ball ending in a bottle depends on the bottle.

Some candidates failed to read “repeatedly thrown until ...” in the question, including “miss” as a possibility in their modelling.

Many candidates seemed to think that “50-50” is a synonym for “of equal probability” in all contexts.

Most candidates handled part (iv) with aplomb, which was very pleasing. A small but significant number tried to answer a more interesting but more difficult question, to simulate whether a ball ends up in a corner bottle, an edge bottle or an inner bottle. It is more difficult because the probabilities have to be computed first from the information in the question. They are 1, 4 and 4 ninths respectively. Credit was allowed for those that did that.

### **Question No. 6**

CPA modelling revolves around producing an activity graph, and that was tested in this question. That necessarily means that there have to be descriptions of the activities, and how they relate to each other. To compensate for this reading burden, the question was arranged so that the resulting graph was as simple as possible, within the constraints of testing the need for dummy activities, et al.

Candidates handled this well in parts (i) and (ii) of the question although, as always, some failed to give the duration and/or critical activities in part (ii).

The following stem, together with parts (iii) and (iv) proved to be a step too far for most candidates. Scheduling is always difficult but very many candidates struggled to demonstrate that they understood what was needed or how to present it. The mark scheme has a row for each task, with shading showing when and who attends to it. It is just as acceptable to have a row for each person, showing when and what they do.

Of course, the problem is that this is not tackled algorithmically, but rather by finding those combinations which use resources most efficiently, and that is not an easy task.

## Unit level raw mark and UMS grade boundaries June 2017 series

For more information about results and grade calculations, see [www.ocr.org.uk/ocr-for/learners-and-parents/getting-your-results](http://www.ocr.org.uk/ocr-for/learners-and-parents/getting-your-results)

### AS GCE / Advanced GCE / AS GCE Double Award / Advanced GCE Double Award

| GCE Mathematics (MEI) |   |     | Max Mark | a  | b  | c  | d  | e  | u |
|-----------------------|---|-----|----------|----|----|----|----|----|---|
| 4751                  | 01 C1 – MEI Introduction to advanced mathematics (AS)   | Raw | 72       | 63 | 58 | 53 | 49 | 45 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4752                  | 01 C2 – MEI Concepts for advanced mathematics (AS)  | Raw | 72       | 55 | 49 | 44 | 39 | 34 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4753                  | 01 (C3) MEI Methods for Advanced Mathematics with Coursework: Written Paper                   | Raw | 72       | 54 | 49 | 45 | 41 | 36 | 0 |
| 4753                  | 02 (C3) MEI Methods for Advanced Mathematics with Coursework: Coursework                      | Raw | 18       | 15 | 13 | 11 | 9  | 8  | 0 |
| 4753                  | 82 (C3) MEI Methods for Advanced Mathematics with Coursework: Carried Forward Coursework Mark | Raw | 18       | 15 | 13 | 11 | 9  | 8  | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4754                  | 01 C4 – MEI Applications of advanced mathematics (A2)   | Raw | 90       | 67 | 61 | 55 | 49 | 43 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4755                  | 01 FP1 – MEI Further concepts for advanced mathematics (AS)                                   | Raw | 72       | 57 | 52 | 47 | 42 | 38 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4756                  | 01 FP2 – MEI Further methods for advanced mathematics (A2)                                    | Raw | 72       | 65 | 58 | 52 | 46 | 40 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4757                  | 01 FP3 – MEI Further applications of advanced mathematics (A2)                                | Raw | 72       | 64 | 56 | 48 | 41 | 34 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4758                  | 01 (DE) MEI Differential Equations with Coursework: Written Paper                             | Raw | 72       | 63 | 56 | 50 | 44 | 37 | 0 |
| 4758                  | 02 (DE) MEI Differential Equations with Coursework: Coursework                                | Raw | 18       | 15 | 13 | 11 | 9  | 8  | 0 |
| 4758                  | 82 (DE) MEI Differential Equations with Coursework: Carried Forward Coursework Mark           | Raw | 18       | 15 | 13 | 11 | 9  | 8  | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4761                  | 01 M1 – MEI Mechanics 1 (AS)  | Raw | 72       | 57 | 49 | 41 | 34 | 27 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4762                  | 01 M2 – MEI Mechanics 2 (A2)  | Raw | 72       | 56 | 48 | 41 | 34 | 27 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4763                  | 01 M3 – MEI Mechanics 3 (A2)  | Raw | 72       | 58 | 50 | 43 | 36 | 29 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4764                  | 01 M4 – MEI Mechanics 4 (A2)  | Raw | 72       | 53 | 45 | 38 | 31 | 24 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4766                  | 01 S1 – MEI Statistics 1 (AS)   | Raw | 72       | 61 | 55 | 49 | 43 | 37 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4767                  | 01 S2 – MEI Statistics 2 (A2)   | Raw | 72       | 56 | 50 | 45 | 40 | 35 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4768                  | 01 S3 – MEI Statistics 3 (A2)   | Raw | 72       | 63 | 57 | 51 | 46 | 41 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4769                  | 01 S4 – MEI Statistics 4 (A2)   | Raw | 72       | 56 | 49 | 42 | 35 | 28 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4771                  | 01 D1 – MEI Decision mathematics 1 (AS)   | Raw | 72       | 52 | 46 | 41 | 36 | 31 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4772                  | 01 D2 – MEI Decision mathematics 2 (A2)   | Raw | 72       | 53 | 48 | 43 | 39 | 35 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4773                  | 01 DC – MEI Decision mathematics computation (A2)   | Raw | 72       | 46 | 40 | 34 | 29 | 24 | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4776                  | 01 (NM) MEI Numerical Methods with Coursework: Written Paper                                  | Raw | 72       | 58 | 53 | 48 | 43 | 37 | 0 |
| 4776                  | 02 (NM) MEI Numerical Methods with Coursework: Coursework                                     | Raw | 18       | 14 | 12 | 10 | 8  | 7  | 0 |
| 4776                  | 82 (NM) MEI Numerical Methods with Coursework: Carried Forward Coursework Mark                | Raw | 18       | 14 | 12 | 10 | 8  | 7  | 0 |
|                       |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| 4777                  | 01 NC – MEI Numerical computation (A2)  | Raw | 72       | 55 | 48 | 41 | 34 | 27 | 0 |

|      |  |     |     |    |    |    |    |    |   |
|------|--|-----|-----|----|----|----|----|----|---|
|      |  | UMS | 100 | 80 | 70 | 60 | 50 | 40 | 0 |
| 4798 | 01 FPT - Further pure mathematics with technology (A2) | Raw | 72  | 57 | 49 | 41 | 33 | 26 | 0 |
|      |  | UMS | 100 | 80 | 70 | 60 | 50 | 40 | 0 |

### GCE Statistics (MEI)

|      |                          |     | Max Mark | a  | b  | c  | d  | e  | u |
|------|--------------------------|-----|----------|----|----|----|----|----|---|
| G241 | 01 Statistics 1 MEI (Z1) | Raw | 72       | 61 | 55 | 49 | 43 | 37 | 0 |
|      |                          | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| G242 | 01 Statistics 2 MEI (Z2) | Raw | 72       | 55 | 48 | 41 | 34 | 27 | 0 |
|      |                          | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| G243 | 01 Statistics 3 MEI (Z3) | Raw | 72       | 56 | 48 | 41 | 34 | 27 | 0 |
|      |                          | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |

### GCE Quantitative Methods (MEI)

|      |   |     | Max Mark | a  | b  | c  | d  | e  | u |
|------|---|-----|----------|----|----|----|----|----|---|
| G244 | 01 Introduction to Quantitative Methods MEI | Raw | 72       | 58 | 50 | 43 | 36 | 28 | 0 |
| G244 | 02 Introduction to Quantitative Methods MEI | Raw | 18       | 14 | 12 | 10 | 8  | 7  | 0 |
|      |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| G245 | 01 Statistics 1 MEI                         | Raw | 72       | 61 | 55 | 49 | 43 | 37 | 0 |
|      |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |
| G246 | 01 Decision 1 MEI                           | Raw | 72       | 52 | 46 | 41 | 36 | 31 | 0 |
|      |   | UMS | 100      | 80 | 70 | 60 | 50 | 40 | 0 |

## Level 3 Certificate and FSMQ raw mark grade boundaries June 2017 series

For more information about results and grade calculations, see [www.ocr.org.uk/ocr-for/learners-and-parents/getting-your-results](http://www.ocr.org.uk/ocr-for/learners-and-parents/getting-your-results)

| Level 3 Certificate Mathematics for Engineering |    |                             |  | Max Mark                              | a* | a | b | c | d | e | u |
|---|----|-----------------------------|--|---------------------------------------|----|---|---|---|---|---|---|
| H860  | 01 | Mathematics for Engineering |  | This unit has no entries in June 2017 |    |   |   |   |   |   |   |
| H860  | 02 | Mathematics for Engineering |  |                                       |    |   |   |   |   |   |   |

| Level 3 Certificate Mathematical Techniques and Applications for Engineers |    |             |     | Max Mark | a* | a  | b  | c  | d  | e  | u |
|--|----|-------------|-----|----------|----|----|----|----|----|----|---|
| H865   | 01 | Component 1 | Raw | 60       | 48 | 42 | 36 | 30 | 24 | 18 | 0 |

| Level 3 Certificate Mathematics - Quantitative Reasoning (MEI) (GQ Reform) |    |  |         | Max Mark | a   | b  | c  | d  | e  | u |
|--|----|--|---------|----------|-----|----|----|----|----|---|
| H866   | 01 | Introduction to quantitative reasoning | Raw     | 72       | 54  | 47 | 40 | 34 | 28 | 0 |
| H866   | 02 | Critical maths                         | Raw     | 60*      | 48  | 42 | 36 | 30 | 24 | 0 |
|  |    |  | Overall | 144      | 112 | 97 | 83 | 70 | 57 | 0 |

\*Component 02 is weighted to give marks out of 72

| Level 3 Certificate Mathematics - Quantitative Problem Solving (MEI) (GQ Reform) |    |  |         | Max Mark | a   | b  | c  | d  | e  | u |
|--|----|--|---------|----------|-----|----|----|----|----|---|
| H867   | 01 | Introduction to quantitative reasoning | Raw     | 72       | 54  | 47 | 40 | 34 | 28 | 0 |
| H867   | 02 | Statistical problem solving            | Raw     | 60*      | 41  | 36 | 31 | 27 | 23 | 0 |
|  |    |  | Overall | 144      | 103 | 90 | 77 | 66 | 56 | 0 |

\*Component 02 is weighted to give marks out of 72

| Advanced Free Standing Mathematics Qualification (FSMQ) |    |                        |     | Max Mark | a  | b  | c  | d  | e  | u |
|---|----|------------------------|-----|----------|----|----|----|----|----|---|
| 6993  | 01 | Additional Mathematics | Raw | 100      | 72 | 63 | 55 | 47 | 39 | 0 |

| Intermediate Free Standing Mathematics Qualification (FSMQ) |    |   |     | Max Mark | a  | b  | c  | d  | e  | u |
|---|----|---|-----|----------|----|----|----|----|----|---|
| 6989  | 01 | Foundations of Advanced Mathematics (MEI) | Raw | 40       | 35 | 30 | 25 | 20 | 16 | 0 |